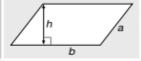
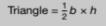
# **GCSE Maths Higher Tier - Formulae**

#### Areas

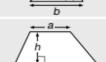




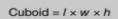




Trapezium =  $\frac{1}{2}(a + b)h$ 



### Volumes





Prism = area of cross section × length



Volume of pyramid =  $\frac{1}{3}$  × area of base × h

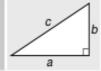
Cylinder =  $\pi r^2 h$ 



## Pythagoras

#### Pythagoras' Theorem

For a right-angled triangle,  $a^2 + b^2 = c^2$ 



#### Trigonometric ratios (new to F)

$$\sin x^{\circ} = \frac{\text{opp}}{\text{hyp}}, \cos x^{\circ} = \frac{\text{adj}}{\text{hyp}}, \tan x^{\circ} = \frac{\text{opp}}{\text{adj}}$$

# hyp opp

## Compound measures

#### Speed

$$speed = \frac{distance}{time}$$



#### Density

density = 
$$\frac{\text{mass}}{\text{volume}}$$



## Quadratic equations

#### The Quadratic Equation

The solutions of  $ax^2 + bx + c = 0$ ,

where  $a \neq 0$ , are given by  $x = \frac{-b \pm \sqrt{(b^2-4ac)}}{2a}$ 

#### Gradient of a Line

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$
or
$$m = \frac{\text{height}}{\text{base}}$$

## Midpoint of two points

Exterior Angles add up to 360°

Angles in Polygons

between 
$$(x_1, y_1)$$
 and  $(x_2, y_2)$   $\left(\frac{x_1 + x_2}{2}, \frac{x_1 + y_2}{2}\right)$ 

Sum of Interior Angles =  $(n-2) \times 180^{\circ}$ 

Where n is the number of sides of the shape

One exterior angle in a REGULAR polygon:

# Equation of a straight Line

Given a point  $(x_1, y_1)$  and the gradient m, the equation of a straight line is

$$y - y_1 = m(x - x_1)$$

Substitute the numbers in, expand and simplify

#### Perpendicular Gradients

Given a gradient of a line m, the gradient of the line perpendicular to it is:  $-\frac{1}{m}$ 

#### Constructing Pie Charts

The angle to draw for each sector is

$$Angle = \frac{frequency}{total} \times 360^{\circ}$$

#### Stratified Sampling

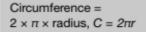
The frequency for a group in a stratified sample is

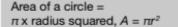
frequency of group total frequency ×sample size

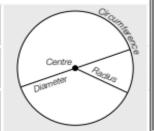
## Pairs of Interior and Exterior Angles add up to 180°

## Circles

Circumference = 
$$\pi \times \text{diameter}$$
,  $C = \pi d$ 







## Area of a Sector

$$A = \frac{\theta}{360^\circ} \! \times \pi r^2$$

Length of an Arc

$$A = \frac{\theta}{360^{\circ}} \times \pi d$$

## Compound Growth & Decay

The amount after n years (or days, etc.) is:

$$\frac{\text{starting}}{\text{amount}} \times \left(1 \pm \frac{r}{100}\right)^n$$

where r is the rate of change. The  $\pm$  means + for growth and – for decay

# Trigonometric formulae

Sine Rule 
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Cosine Rule 
$$a^2 = b^2 + c^2 - 2bc \cos A$$

Area of triangle = 
$$\frac{1}{2}$$
 ab sin C

